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$$(l^\infty(\mathbb{R}), +, \cdot, \| \cdot \|_\infty)$$

Definition.

$$l^\infty(\mathbb{R}) := \{\alpha : \mathbb{N} \rightarrow \mathbb{R} : |\alpha_i| \leq K, \forall i\}$$

and

$$\|(a_n)\|_\infty := \sup\{|a_n|, n \in \mathbb{N}\}$$



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is a vector subspace of $\mathbb{R}^\mathbb{N}$ where $\| \cdot \|_\infty$ is a norm on the space.

• $\|a_n + b_n\|_\infty$

- $|a_k - b_k| \leq |a_k| + |b_k|$
- So,

$$\|a_n + b_n\|_\infty \leq \|a_n\|_\infty + \|b_n\|_\infty$$

Current note has 0 direct children and 0 total descendants.

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 - $l^\infty(\mathbb{R})$

And it has 39 siblings.

- [stem](#)
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