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Euler's iterative solution method for first order ODEs

For

$$\begin{aligned}y' &= F(x, y) \\ y(0) &= \alpha\end{aligned}$$

we

Naive calculations

$$y(x+h) = y(x) + hF(x, y(x))$$

Definition. Euler's iteration

Divide $[0, L]$ into n partitions $x_i = ih, i \in \{0, \dots, n\}$ of length h

$$\begin{aligned}y_0 &:= \alpha \\ y_{i+1} &:= y_i + hF(x_i, y_i)\end{aligned}$$

[1]

convergence

Let

$$i \in \{0, \dots, n\} \implies |E_{i+1}| \leq A^i |E_0| + B$$

then

$$i \in \{0, \dots, n\} \implies |E_i| \leq A^i |E_0| + \frac{A^i - 1}{A - 1} B$$

Let Y_k be the actual solution, then

$$E_k := Y_k - y_k$$

Now consider

$$\begin{aligned}|E_{k+1}| &= |Y_{k+1} - y_{k+1}| \\ &= |Y(x_k + h) - (y_k + hF(x_k, y_k))|\end{aligned}$$

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And it has 10 siblings.

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