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Local transformation rules

on a	section/object, globally	locally it looks like	transformation rule	connection, locally	derivative using the connection	connection transforms	derivative transform
manifold M with local charts (Φ_α, U_α)	smooth map $f : M \rightarrow \mathbb{R}$	on U_α $f_\alpha : U_\alpha \rightarrow \mathbb{R}$	on $U_\alpha \cap U_\beta$ $f_\alpha = f_\beta$ "doesn't transform"	$\nabla f = df$	$X^i \frac{\partial f}{\partial x_i}$		
$g_{\alpha\beta} := \mathfrak{D}(\phi_\alpha, \phi_\beta)$	a tangent vector field $X : M \rightarrow T(M)$	on U_α $X = X_\alpha^i \frac{\partial}{\partial x_\alpha^i}$ where $X_\alpha : U_\alpha \rightarrow T(U_\alpha)$	on $U_\alpha \cap U_\beta$ $g_{\alpha\beta}(X_\alpha) = g_{\beta\alpha}(X_\beta)$				
	a smooth map $f : M \rightarrow V$						
$\mathbb{R}$ -vector bundle $E \rightarrow M$ of rank n with local trivializations on V_α transition maps $g_{\alpha\beta} : V_\alpha \cap V_\beta \rightarrow GL(n, \mathbb{R})$	a smooth section $\phi : M \rightarrow E$	on V_α $\phi_\alpha : V_\alpha \rightarrow E _{V_\alpha}$	on $V_\alpha \cap V_\beta$ $g_{\alpha\beta}(\phi_\beta) = \phi_\alpha$ which is a matrix multiplication	on U_α $\nabla = d + A_\alpha$ where $A_\alpha \in \Omega^1(U_\alpha)$	$\nabla \phi_\alpha = d\phi_\alpha + A_\alpha(\phi_\alpha)$	$A_\alpha = g_{\beta\alpha}^{-1}(\phi_\beta)$	
$\mathbb{R}$ -line bundle $L \rightarrow M$ with local trivializations on V_α transition maps $g_{\alpha\beta} : V_\alpha \cap V_\beta \rightarrow \mathbb{R}^\times$	a smooth section $\phi : M \rightarrow L$	on V_α $\phi_\alpha : V_\alpha \rightarrow L _{V_\alpha}$	on $V_\alpha \cap V_\beta$ $g_{\alpha\beta} \phi_\beta = \phi_\alpha$ which is <i>just</i> real numbers multiplication				
	a smooth map $f : M \rightarrow \mathbb{C}$		$f_\alpha = f_\beta$	$\nabla f = df$			
$\mathbb{C}$ -line bundle with local trivializations on V_α transition maps $g_{\alpha\beta} : V_\alpha \cap V_\beta \rightarrow \mathbb{C}^\times$			on $V_\alpha \cap V_\beta$ $g_{\alpha\beta} \phi_\beta = \phi_\alpha$ which is <i>just</i> complex numbers multiplication	on U_α $\nabla = d + A_\alpha$			
a G -bundle $P \rightarrow M$ and a associated bundle $E \rightarrow M$	a smooth section $\phi : M \rightarrow E$			on U_α $\nabla = d + A_\alpha$ where $A_\alpha \in \Omega^1(U_\alpha)$			

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- [structures based on sets](#)
 - [manifolds](#)
 - [smooth \$\mathbb{R}\$ -manifold](#)
 - [Local transformation rules](#)

And it has 19 siblings.

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 - [manifolds](#)
 - [smooth \$\mathbb{R}\$ -manifold](#)

- [Smooth Lie group action on a smooth manifold](#)
- [Borel measures on a smooth manifold](#)
- [\$G\$ -bundles over smooth manifolds \$G \curvearrowright P \rightarrow X\$](#)
- [Vector bundle on smooth manifolds](#)
- [Curves in smooth manifolds](#)
- [Density on smooth manifolds](#)
- [Functions between smooth manifolds](#)
- [Functions from smooth manifolds to \$\mathbb{R}\$](#)
- [Flows on a smooth manifold](#)
- [Locally \$G \curvearrowright X\$ -manifolds](#)
- [Smooth singular homology of a smooth manifold](#)
- [Isomorphisms and automorphisms of smooth manifolds](#)
- [Lagrangian flows](#)
- [Local transformation rules](#)
- [Moduli space of Riemannian metrics on a smooth manifold](#)
- [Moduli space of quotients](#)
- [Quotient manifolds](#)
- [Submanifolds of smooth manifolds](#)
- [Tangents on a smooth manifold](#)