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# $\mathbb{R} \times S^2$

#wiki/Man/R/3

- diffeomorphism

$$\begin{aligned} \mathbb{R}^3 \setminus \{(0,0,0)\} &\cong \mathbb{R} \times S^2 \\ x &\mapsto \left(\log \|x\|, \frac{x}{\|x\|}\right) \\ (e^\theta p) &\leftrightarrow (\theta, p) \end{aligned}$$

- product Riemannian metric  $S^2 \oplus \mathbb{R}$ 
  - exactly 4 compact manifolds with  $S^2 \oplus \mathbb{R}$  geometry
    - $S^2 \times S^1$
    - $\mathbb{R}P^2 \times S^1$
    - $M_2$
    - $\mathbb{R}P^3 \# \mathbb{R}P^3$
- simply connected
  - $\implies$  has no complete constant curvature metric

Current note has 0 direct children and 0 total descendants.

- [stretchy](#)
  - $\mathbb{R} \times S^2$

And it has 62 siblings.

- [stretchy](#)
  - [Trefoil 3<sub>1</sub> knot](#)
  - [The only compact connected Lie group that can act faithfully on a torus is itself](#)
  - [Hecke algebras](#)
  - $\overline{B^n}$
  - $\text{BS}(1,2)$
  - $(\mathbb{C}, +, \times)$
  - $D^* := D \setminus \{0\}$
  - [Cantor set](#)
  - [Configuration space of  \$N\$  rigid points in  \$\mathbb{R}^3\$](#)
  - [Free groups](#)
  - $GL(2)(\mathbb{Z}) \curvearrowright T^2$
  - $H^3_2$
  - $[a,b]$
  - [Figure 8 knot](#)
  - [Lamplighter group on  \$\mathbb{Z}\_2\$](#)
  - $\beta\mathbb{N}$
  - $\#_2\mathbb{R}P^2$
  - $\prod_{i \in \mathbb{N}} \{1, \dots, n_i\}$
  - $\mathbb{R}P^n$
  - $(\mathbb{Q}, +, \times, <)$
  - $\mathbb{Q}_{\hat{p}}$
  - $\overline{\mathbb{Q}}$
  - $\mathbb{Q}_{\text{constr}}$
  - $\mathbb{Q}(\xi_n)$
  - $\mathcal{O}_{\overline{\mathbb{Q}}}$
  - $(\mathbb{R}, +, \times, <, \sup)$
  - [Homeomorphism of  \$\mathbb{R}^2\$  that sends  \$\mathbb{N}\$  to a countable closed discrete subset](#)
  - $\mathbb{R}^2 \times S^1$
  - $\mathbb{R}^n$
  - $\mathbb{R} \times S^1$
  - $\mathbb{R} \times S^2$
  - $S^1$
  - $S^1 \wedge S^1$
  - $S^1 \times S^n$
  - [S<sup>2</sup> and  \$\mathbb{C}P^1\$](#)
  - [Mapping torus of the antipodal map of  \$S^2\$](#)
  - $S^3$
  - $S^n$
  - [I-bundle](#)
  - [Symmetric group](#)
  - $\mathbb{I}$
  - $T^2$
  - $T^2_g$
  - $T^2_{0,0,3}$
  - $\mathbb{R}^2 \setminus \{0\}$
  - [Three  \$T^2\_{1,0,1}\$ -glued at their boundaries](#)
  - $T^2_{1,1,0}$
  - $T^2_2$

- $T_g^2 \times [0,1]$
- $\#_{\mathbb{N}} T^2$
- Thompson's group
- $T^n$
- 3-valent tree
- 4-valent tree
- $[0,1]^{\mathbb{N}}$  with product topology.
- Whitehead manifolds
- $\mathbb{Z}$
- $\mathbb{Z}[\sqrt{m}]$
- $\mathbb{Z}[X]$
- $\mathbb{Z}^{\mathbb{N}}$
- $\mathbb{Z}[i]$
- $\mathbb{Z}[i\sqrt{5}]$