ⓘ Info

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$\mathbb{Z}^{\mathbb{N}}$

Consider the set of all sequences in $\mathbb{Z}$

$$\mathbb{Z}^{\mathbb{N}}$$

which is an uncountable $\mathbb{Z}$-algebra.

We have a $\mathbb{Z}$-algebra homomorphism

$$\begin{aligned} \mathcal{C}_0(\mathbb{Z}) &\hookrightarrow \mathbb{Z}^{\mathbb{N}} \\ p &\mapsto p|_{\mathbb{N}} \end{aligned}$$

which is obviously not surjective because $\mathcal{C}_0(\mathbb{Z}) \cong_{\mathsf{Mod}_{\mathbb{Z}}} \mathbb{Z}[X]$ is countable.

Current note has 0 direct children and 0 total descendants.

- stretchy
  - $\mathbb{Z}^{\mathbb{N}}$

And it has 62 siblings.

- stretchy
  - Trefoil 3_1 knot
  - The only compact connected Lie group that can act faithfully on a torus is itself
  - Hecke algebras
  - $\overline{B^n}$
  - $\mathrm{BS}(1,2)$
  - $(\mathbb{C},+,\times)$
  - $D^* := D \setminus \{0\}$
  - Cantor set
  - Configuration space of N rigid points in $\mathbb{R}^3$
  - Free groups
  - $GL(2)(\mathbb{Z}) \curvearrowright T^2$
  - H^3_2
  - $[a,b]$
  - Figure 8 knot
  - Lamplighter group on $\mathbb{Z}_2$
  - $\beta\mathbb{N}$
  - $\#_2\mathbb{R}P^2$
  - $\prod_{i\in\mathbb{N}}\{1,\ldots,n_i\}$
  - $\mathbb{R}P^n$
  - $(\mathbb{Q},+,\times,<)$
  - $\mathbb{Q}_{\hat{p}}$
  - $\overline{\mathbb{Q}}$
  - $\mathbb{Q}_{\mathrm{constr}}$
  - $\mathbb{Q}(\xi_n)$
  - $\mathcal{O}_{\overline{\mathbb{Q}}}$
  - $(\mathbb{R},+,\times,<,\sup)$
  - Homeomorphism of $\mathbb{R}^2$ that sends $\mathbb{N}$ to a countable closed discrete subset
  - $\mathbb{R}^2\times S^1$
  - $\mathbb{R}^n$
  - $\mathbb{R}\times S^1$
  - $\mathbb{R}\times S^2$
  - S^1
  - $S^1\wedge S^1$
  - $S^1\times S^n$
  - S^2 and $\mathbb{C}P^1$
  - Mapping torus of the antipodal map of S^2
  - S^3
  - S^n
  - I-bundle
  - Symmetric group
  - $\mathbb{T}$
  - T^2
  - T^2_g
  - $T^2_{0,0,3}$
  - $\mathbb{R}^2\setminus\{0\}$
  - Three $T^2_{1,0,1}$-glued at their boundaries
  - $T^2_{1,1,0}$
  - T^2_2
  - $T^2_g\times[0,1]$
  - $\#_{\mathbb{N}}T^2$
  - Thompson's group
  - T^n
  - 3-valent tree
  - 4-valent tree

- $[0, 1]^{\mathbb{N}}$ with product topology
- Whitehead manifolds
- $\mathbb{Z}$
- $\mathbb{Z}[\sqrt{m}]$
- $\mathbb{Z}[X]$
- $\mathbb{Z}^{\mathbb{N}}$
- $\mathbb{Z}[i]$
- $\mathbb{Z}[i\sqrt{5}]$