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Functions with uniformly bounded mean oscillations on cubes

 **Definition. Functions with uniformly bounded mean oscillations on cubes**

Let $f \in L^1_{\text{loc}}(\mathbb{R}^d)$ and

$$\|f\|_{\text{BMO}} := \sup \left\{ \frac{1}{m(R)} \int_R \left| f - \frac{1}{m(R)} \int_R f \right| \middle| R \text{ is a cube in } \mathbb{R}^d \right\}$$

and

$$\text{BMO} := \frac{\{f \in L^1_{\text{loc}}(\mathbb{R}^d) \mid \|f\|_{\text{BMO}} < \infty\}}{\{\text{functions that are constant aeon } \mathbb{R}^d\}}$$

Proposition:

$$L^\infty \rightarrow \text{BMO}$$

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And it has 15 siblings.

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 - [Rf](#) subobjects of and functions on $\mathbb{R}^n, T^n, S^n, \mathbb{C}^n$
 - [Lmeas](#) Lebesgue measurable subsets of and functions on \mathbb{R}^n, T^n, S^n
 - [BMO](#) Functions with uniformly bounded mean oscillations on cubes
 - [decom bd](#) Chebyshev's inequality
 - [decom CZ](#) Calderon-Zygmund decomposition
 - [density](#) Lebesgue density of measurable sets
 - [DMO](#) Functions with uniformly bounded mean oscillations on dyadic cubes
 - [End int](#) Volterra operator $\int_{[0,-]}^1 : L_{loc}^1[0, 1] \rightarrow \mathcal{C}[0, 1]$
 - [f](#) Measurable functions on \mathbb{R}^n
 - [f quant](#) (ϵ, n) -measurable function
 - [int](#) Integrability and integral of measurable functions on \mathbb{R}^n
 - [int HL](#) Hardy-Littlewood maximal functions of $L_{loc}^1(\mathbb{R}^n)$
 - [int mean](#) Lebesgue averaging and differentiation
 - [int monotone](#) Integrals of a monotonically converging sequence of functions
 - [int undergraph](#) Lebesgue integral from measure of undergraph
 - [Lorentz](#) $L^{p,q}$
 - [unit mass](#) $E([0, 1]) = E(0, 1), E([- \pi, \pi]) = E(S^1)$