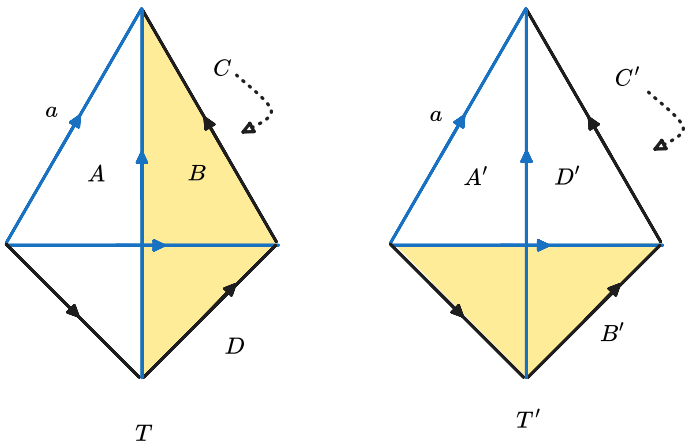


This note, that [was found here](#), as a part of [a collection](#) is written (completely with human hands) by [Rupadarshi Ray](#), was created on March 7, 2026 9:03:41 PM, was last modified on March 8, 2026 4:25:35 PM, and was exported on September 7, 2026 3:04:02 PM.

## Complement of the figure 8 knot in $S^3$

Definition. Definition



Let  $S \in \{A, B, C, D\}$  be a face of  $T$  and

$$f_S : T' \rightarrow T \in \text{Isom}(\mathbb{R}H^3)$$

be the unique orientation reversing isometry that maps

$$S \mapsto S'$$

Let  $g_S$  be  $f_S$  followed by a reflection in the side  $S$ . Then

$$\{g_A, g_B, g_C, g_D, g_A^{-1}, g_B^{-1}, g_C^{-1}, g_D^{-1}\}$$

form a side pairing for  $T, T'$ . We consider the orientable hyperbolic 3-manifold

$$\frac{T \sqcup T'}{g_A, g_B, g_C, g_D, g_A^{-1}, g_B^{-1}, g_C^{-1}, g_D^{-1}}$$

```
import snappy
M = snappy.Manifold("m004")
print("Link complement of ",snappy.LinkExteriors.identify(M))
print("Is orientable: ",M.is_orientable())
print("Is hyperbolic:", M.solution_type())
# print(M.alexander_polynomial())
print("Volume:", M.volume())

T= snappy.Triangulation(M)
print(T.num_tetrahedra())
print(T.gluing_equations())

print("Fundamental group presentation:")
G =
M.fundamental_group(minimize_number_of_generators=True,simplify_presentat
ion=True)
print(G)
for i in 'abcd':
    print(i,G.SL2C(i))
print(M.dirichlet_domain())
# M.dirichlet_domain().view()
print("Homology: ",M.homology())

# print(M.identify())
# print(M.length_spectrum(0.75, include_words=True))
```

[1]

Current note has 0 direct children and 0 total descendants.

- stretchy
  - Figure 8 knot
    - Complement of the figure 8 knot in  $S^3$

And it has 1 siblings.

- stretchy
  - Figure 8 knot
    - Complement of the figure 8 knot in  $S^3$

1. [John G. Ratcliffe - Foundations of Hyperbolic Manifolds \(2019\),\\_p.447](#) ↩